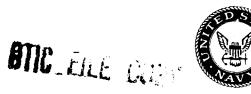


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Time-Dependent Slow-Time-Scale Theory of Free-Running and Phase-Locked Gyrotron Oscillators

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TIME-DEPENDENT SLOW-TIME-SCALE THEORY OF FREE-RUNNING AND PHASE-LOCKED GYROTRON OSCILLATORS

I. INTRODUCTION

There is currently considerable interest in the development of high power phase-locked gyrotron oscillators. These devices have the potential to combine the high efficiency and power associated with oscillators with the coherence and phase control properties associated with amplifiers. Although previous theoretical work on gyrotron operation[1-8] has been successfully applied to the development of cw devices for heating of tokamak plasmas, the investigation of phase-locked gyrotron operation, particularly involving pulse-line accelerator driven devices, presents a new challenge to the theorist. These devices, based on intense relativistic electron beams, are characterized by short pulselengths and voltage risetime and ripple effects which can prevent the establishment of a steady-state equilibrium. consideration of non-stationary operation is also involved in the investigation of conditions for phase-locked operation. Timedependent effects can be studied using a particle-in-cell simulation code of the type developed by Lin and co-workers[9]. In this work an alternative slow-time-scale approach is used to obtain a relatively simple, economical analysis of the timedependent, nonlinear dynamics of pulsed gyrotrons.

The time-dependent theory of gyrotrons has been considered by Nusinovich and co-workers[10,11], mainly in the context of

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multimode operation and mode stability. A time multimode theory of quasi-optical gyrotrons has been developed by Bondeson et al.[12]. Early work on mode selection and phase-locking of vacuum tube oscillators was carried out by Van der Pol[13] and Adler[14]. An analytical theory of the conditions for phaselocking gyrotrons has been presented by Manheimer[15,16]. emphasis in the present work is on the modeling of transient effects in gyrotrons whose pulse length is only a few times longer than the characteristic risetime of cavity fields. The approach is developed for the case of several interacting modes with closely spaced frequencies and interacting at the same harmonic of the cyclotron frequency. Calculations are presented for single mode operation of relativistic gyrotron with parameters similar to an experimental device under test at the Naval Research Laboratory[17]. Both free-running and phaselocked operation are considered. The phase-locking signal is introduced via a prebunched beam. The effect of a voltage ripple is investigated. The possibility of phase-locked operation in the presence of voltage ripple - an important issue for proposed NRL experiments - is demonstrated. Calculations for multimode operation will be the subject of future work.

The time theory of gyrotron oscillators derived in this work is based on slow-time-scale equations for the electron motion similar to those used in steady-state models[7,18,19]. Slow-

time-scale equations for the cavity rf field amplitude are obtained by expressing the time-dependant behavior relative to a reference frequency ω_o which is close to the operating frequency ω . The next section of this paper contains an outline of the theoretical approach. The third section contains the results of calculations and the last section presents some conclusions drawn from this research.

II. THEORY

Consider a gyrotron with a cylindrical resonator and a thin annular beam. The electrons follow helical trajectories in the applied axial magnetic field about guiding centers located at a radius $R_{\rm o}$ from the symmetry axis. The electron beam interacts with one or more resonator modes, which are assumed to be TE modes with closely spaced oscillation frequencies. It is convenient to look at time effects which remain after a reference frequency $\omega_{\rm o}$ has been factored out. These effects are characterized by time scales which are much longer than the wave period and are incorporated in time mode amplitudes $A_{\rm n}$ (t). The total transverse electric field is expressed in the form

$$E_{t} = \sum_{n=1}^{N} A_{n}(t)h_{n}(z)e_{n}(r,\theta;z)exp(-i\omega_{o}t)$$
 (1)

where \mathbf{e}_{n} is a transverse mode vector function defined in Ref. 18, and $\mathbf{h}_{n}\left(\mathbf{z}\right)$ is an axial profile function which satisfies the Helmholtz equation;

$$\left[\frac{d^{2}}{dz^{2}} + k_{zn}^{2}\right] h_{n}(z) = 0$$
 (2)

The function $P_n = h_n e_n$ is an eigenfunction of the empty resonator in the single transverse mode approximation with eigenfrequency ω_{no} . Thus the present formulation neglects beam loading effects on the mode axial profile. N is the number of interacting modes. The slowly varying mode amplitudes have the form:

$$A_n(t) = f_n(t)e^{-i\psi_n(t)}$$
(3)

The phase derivative $\psi_n'=d\psi_n/dt$ corresponds to the frequency difference between the mode oscillation frequency ω_n and ω_o . The transverse electric field satisfies the wave equation:

$$\nabla^2 \mathbf{E}_{t} - \frac{1}{C^2 \partial t^2} = \mu_o \frac{\partial \mathbf{J}_{t}}{\partial t} \tag{4}$$

where J_t is the transverse ac current density, c is the speed of light and μ_o is the permeability of free space. MKS units are used throughout except as noted. Substituting Eq.(1) into Eq.(4), introducing a mode Q factor, Q_n , to account for diffraction and ohmic losses, and noting that $dA_n/dt << \omega_o A_n$ one obtains

$$\sum_{n=1}^{N} e^{-i\omega_{o}t} \left[(\omega_{o}^{2} - \omega_{no}^{2}) A_{n} + \frac{i\omega_{no}^{2}}{Q_{n}} A_{n} + 2i\omega_{o} \frac{dA_{n}}{dt} \right] h_{n} e_{n} = c^{2} \mu_{o} \frac{\partial J_{t}}{\partial t}$$
(5)

where ω_{no} is the empty resonator eigenfrequency for the nth mode. Multiplying Eq.(5) on both sides by $(h_n e_n)^*$, integrating over the cavity volume and applying the orthogonality properties of the transverse vector functions[18] leads to the mode excitation equation:

$$\left[\frac{d}{dt} + \frac{\omega_o}{2Q_n} - i(\omega_o - \omega_{no})\right] A_n(t) = -\frac{ic^2 \mu_o}{2N_n \omega_o} \int_{V} dz da \ h_n^* e_n^* \cdot \frac{\partial J_t}{\partial t} e^{i\omega_o t}$$
(6)

where N_n is the axial mode normalization integral:

$$N_n = \int_0^L dz |h_n(z)|^2$$
 (7)

To evaluate the right hand side of Eq.(6) the rf current density is written in the approximate form[7]:

$$\mathbf{J}_{t} = \mathbf{J}_{\omega_{o}} \exp(-i\omega_{o} t) \tag{8}$$

where

$$\mathbf{J}_{\omega_{o}} = \int_{0}^{2\pi} \mathbf{d}(\omega_{o} t) \mathbf{J}_{t} e^{i\omega_{o} t}$$
(9)

Introducing the normalized frequency shift $\delta_n = (\omega_o - \omega_{no})/\omega_o$ and time $\tau = \omega_o$ t and substituting Eq.(8) into Eq.(6) leads to:

$$\left[\frac{d}{d\tau} + \frac{1}{2Q_n} - i\delta_n\right] A_n(\tau) = -\frac{c^2 \mu_n}{2N_n \omega_n} \int_{\gamma} dz da \ h_n^* e_n^* \cdot J_{\omega_n} e^{-i\Psi_n}$$
(10)

To calculate the ac current density, the interaction with the electron beam is treated in the single particle approximation. A considerable simplification of the general time-dependent problem results if one uses the fact that the characteristic rise-time of fields in the resonator is much longer than the electron transit time in the cavity. In this case one can use a quasi-steady-state approximation in which the electron trajectories are calculated for rf fields with fixed amplitude, cos_{3} , and linearized phase, $\psi_{n} \simeq \psi_{n} ' (\tau_{o}) (\tau - \tau_{o})$. The slow-time-scale nonlinear electron equations of motion for a particular harmonic are readily deduced from previous steady-state analyses[7,18] and are given by:

$$\frac{d\mathbf{u}_{t}}{d\bar{z}} = -\frac{\gamma}{\mathbf{u}_{z}^{N}} \sum_{n=1}^{N} \mathbf{F}_{n} \mathbf{J}_{S}'(\bar{\mathbf{k}}_{n} \bar{\mathbf{r}}_{L}) \operatorname{Re} \left[\left(\mathbf{h}_{n} + i \frac{\mathbf{u}_{z}}{\gamma \bar{\omega}_{o}} \frac{d\mathbf{h}_{n}}{d\bar{z}} \right) e^{-i \left[\Lambda + \psi_{n} - (\mathbf{m}_{n} - s) \Xi_{o} \right]} \right]$$
(11a)

$$\frac{d\Lambda}{d\bar{z}} = -\frac{s\gamma}{u_z u_t} \sum_{n=1}^{N} F_n \frac{sJ_s(\bar{k}_n \bar{r}_L)}{\bar{k}_n \bar{r}_L} Re \left[\left(h_n + i \frac{u_z}{\gamma \bar{\omega}_o} \frac{dh_n}{d\bar{z}} - \frac{\bar{\omega}_{no}^2 u_t^2}{s \bar{\omega}_o \gamma} h_n \right) \right]$$

$$e^{-i \left[\Lambda + \psi_n - (m_n - s) \Xi_o \right] + \bar{\omega}_o \left(1 - \frac{s \bar{\Omega} \gamma_o}{\bar{\omega}_o \gamma} \right) \qquad (11b)$$

$$\frac{du_z}{d\bar{z}} = \frac{u_t}{u_z \bar{\omega}_o} \sum_{n=1}^{N} F_n J_s'(\bar{k}_n \bar{r}_L) Re \left[i \frac{dh_n}{d\bar{z}} e^{-i \left[\Lambda + \psi_n - (m_n - s) \Xi_o \right]} \right] \qquad (11c)$$

where $u_t = \gamma v_t/c$ is the normalized transverse momentum amplitude, $u_x = \gamma v_x/c$ is the normalized axial momentum, Λ is a slowly varying transverse momentum phase, s is the harmonic number, m_n is the mode azimuthal index, γ is the relativistic mass ratio, k_n is the mode transverse wavenumber, r_t is the Larmor radius of the orbit, J_s (J_s') is (the derivative of) a regular Bessel function, Q is the relativistic cyclotron frequency corresponding to the input beam energy, Ξ_o is the orbit guiding center azimuthal angle, and F_n is the normalized rf field amplitude:

$$F_{n} = \frac{|e|}{m_{e} c^{2}} \frac{J_{m_{n}} - s^{(k_{n} R_{e})}}{\sqrt{[\pi(1 - m_{n}^{2}/x_{n}^{\prime 2})]J_{m_{n}}(x_{n}^{\prime})}} f_{n}$$
 (12)

Quantities with a "-" have been normalized according to: $\overline{z} = z/r_{wo}, \ \overline{r}_L = r_L/r_{wo}, \ \overline{\varrho} = \varrho r_{wo}/c, \ \overline{\omega}_o = \omega_o r_{wo}/c, \ \text{and} \ \overline{k}_n = k_n r_{wo}. \ R_o$ denotes the orbit guiding center radius, e is the electron charge, m_o is the electron mass, x_n' is a zero of J_m' for the mode n, and r_{wo} is an arbitrary normalization length usually chosen to be a representative cavity wall radius.

The ac current density is obtained by integrating Eqs.(11) for an appropriate set of initial conditions at the cavity input at z_o . For a cold, phase-mixed electron beam: $u_t(z_o)=u_{to}$, $u_z(z_o)=u_{zo}$, and $\Lambda(z_o)=\Lambda_o$ is uniformly distributed in the interval $[0,2\pi]$. The case of an electron beam prebunched by passage

through a bunching cavity driven at a frequency ω_{o} can be modeled by an initial phase angle distribution of the form:

$$\Lambda_{o} = \Theta_{o} + q_{B} \sin \Theta_{o} - \Phi_{o} \tag{13}$$

where Θ_o is uniformly distributed in the interval $[0,2\pi]$, q_B is the bunching parameter, and Φ_o is an initial phase. For an annular beam, Eqs.(11) are averaged with respect to Ξ_o . For a thin annular beam the transverse ac current density is given by

$$\mathbf{J}_{t} = -\frac{\mathbf{I}_{o}}{\mathbf{v}_{z}}\mathbf{v}_{t} \tag{14}$$

Substitution of Eqs.(14) and (9) into Eq.(10) leads to the following equations for the mode amplitude and phase:

$$\frac{dF_{n}}{d\tau} = Re \left(I \int d\bar{z} h_{n}^{*} \langle \frac{u_{t}}{u_{z}} J_{s}'(\bar{k}_{n} \bar{r}_{L}) e^{i[\Lambda + \psi_{n} - (m_{n} - s)\Xi_{o}]} \rangle_{\Lambda_{o}, \Xi_{o}} \right) - \frac{F_{n}}{2Q_{n}}$$
(15a)

$$\frac{d\psi_{n}}{d\tau} = -\delta_{n} - Im \left[I \int d\overline{z} h_{n}^{\star} \langle \frac{u_{t}}{u_{z}} J_{s}^{\prime} (\overline{k}_{n} \overline{r}_{L}) e^{i [\Lambda + \psi_{n} - (m_{n} - s) \Xi_{o}]} \rangle_{\Lambda_{o}, \Xi_{o}} \right]$$
(15b)

where I is the normalized current parameter:

$$I = \frac{|e|\mu_{o}}{m_{o} c \overline{\omega}_{o}} \frac{r_{wo} J_{m-s}^{2}(k_{n} R_{o})}{\pi (1-m^{2}/x_{n}^{\prime 2}) J_{m}^{2}(x_{n}^{\prime}) N_{n}} I_{o}$$
 (16)

and $\langle \; \rangle_a$ denotes an average with respect to the variable a. The time behavior of a free-running or driven gyrotron oscillator is obtained by solving Eqs.(15) together with (11) subject to appropriate initial conditions as discussed above. When the phase ψ_n of a driven oscillator (via beam prebunching) converges to a constant value, the oscillator is said to be phase-locked. The locking frequency is ω_o in the present formulation. When the interaction occurs with only a single circularly polarized mode, the ac current density averaged with respect to Λ_o is independent of the guiding center azimuthal position so that the average with to Ξ_o may be omitted.

III. RESULTS

Calculations have been carried for a high voltage 35 GHz gyrotron configuration similar to the NRL experiment recently reported by Gold et al.[17]. The peak voltage and current of the annular beam are taken to be 650 kV and 1.5 kA, respectively. The beam guiding center radius is $R_0 = 1.16$ cm, the cavity radius is 1.6 cm, and the longitudinal profile of the cavity fields is assumed to be sinusoidal with length 4 cm. The operating mode is the TE,,, circular mode with polarization counter-rotating to the beam rotation. The beam pitch ratio $\alpha = v_{+}/v_{z} = 1$. The cavity Q factor Q=250. The applied magnetic field is 2.4 Tesla. Spreads in beam guiding center and pitch ratio are neglected as are space-charge effects. In these calculations the cavity is seeded with low amplitude rf fields (1 kV/cm at the beam in the present case). The results of calculations for free-running and phaselocked oscillator operation are presented below. The effect of a voltage ripple is shown.

The first set of calculations correspond to an idealized 50 nsec voltage pulse with a 3 nsec rise from 75% of peak to peak voltage and no ripple. The beam current and pitch ratio are assumed to vary linearly with voltage and as $V^{1.33}$, respectively, during the voltage rise up to the maximum values given above. Results for the free-running oscillator are shown in Figures 1 (a)-1(c). These Figures show, respectively, the electronic

efficiency, operating frequency, and rf phase of the oscillator plotted as a function of time. Figure 1(b) plots the shift in operating frequency ω relative to ω_o which is taken to be the the cold cavity eigenfrequency (which is close to 35 GHz). These plots indicate that steady-state operation is achieved after about 8 nsec. The steady-state efficiency is 17.7%, corresponding to an output power of 173 MW, and the steady-state frequency shift $\delta_{FR} = (\omega_{FR} - \omega_o)/\omega_o$ due to beam loading is 5.5×10^{-4} which corresponds to 19.2 MHz. This frequency shift leads to a linearly increasing rf phase with time as shown in Figure 1(c).

Results for an oscillator driven via a prebunched beam are given in Figures 2(a)-2(c). The beam is modulated at a frequency ω_o and the modulation amplitude is modeled by the bunching parameter $q_B=0.5$. An estimate for the locking signal power required to obtain a beam with $q_B=0.5$ is given below. In this calculation the difference between the normalized locking signal frequency and the normalized free-running oscillator (FRO) frequency is $\delta_L=(\omega_o-\omega_{FR})/\omega_o=1.05\times10^{-3}$ or $\Delta f=35$ MHz. Figures 2(b) and 2(c) show that phase-locked operation is obtained after 30 nsec into the voltage pulse. The phase-locked condition is indicated by a frequency shift $\omega-\omega_o=0$ and constant rf phase. As shown in Figure 2(a), in this case the oscillator efficiency is reduced slightly to 16% while phase-locked.

If the difference between the locking signal frequency and the FRO frequency Δf is too large, phase-locking will not occur. Instead a periodic perturbation of the oscillator behavior is observed as shown in Figures 3(a)-3(c). The locking signal detuning in this case is δ_L =1.55×10⁻³ or Δf =54 MHz. The beat frequency of the perturbation is about 28 MHz. The non-phase-locked behavior of the rf phase is clearly shown by Fig. 3(c).

The case of a FRO with a voltage ripple is shown in Figures 4(a)-4(c). The voltage ripple amplitude is 2% and the ripple period is 10 nsec. Other parameters are the same as for the FRO case discussed above. Figures 4(a) and 4(b) show that this voltage ripple causes a 3.4% amplitude ripple in the efficiency and a 0.06% amplitude ripple (21 MHz) in the frequency. Figures 5(a)-5(b) show the results of driving this oscillator configuration with a prebunched beam with $q_{\rm B}\!=\!0.5$ and modulation frequency shift $\delta_{\rm L} = 5.5 \times 10^{-4}$ (19 MHz). Figures 5(b) and 5(c) show that phase-locked operation is achieved in the sense that after about 30 nsec the oscillation frequency averaged over the ripple period equals the drive frequency and the averaged rf phase angle is a constant. As in the FRO, the voltage ripple leads to a 0.06% frequency ripple in the PLO. The frequency ripple causes a corresponding 13° amplitude ripple in the phase angle. Figures 6(a)-6(c) represent the case of an unphase-locked, driven oscillator with a 2% voltage ripple. The drive signal frequency

shift is $\delta_L = 2.5 \times 10^{-3}$ (88 MHz). The beat frequency for the perturbed oscillator is about 34 MHz. The failure to achieve phase-locked operation is clearly shown by the phase angle plotted in Figure 6(c).

To estimate the input power needed to obtain a beam bunching parameter $q_B = 0.5$ for circularly polarized radiation and a gaussian rf profile in the bunching cavity, one can apply the small signal gyroklystron theory developed by Tran et al [20]. The required input power in Watts is:

$$P_{in}(W) = \frac{\sqrt{\pi c^3 m_o^2 (x_n'^2 - m^2) J_m^2 (x_n') \gamma_o^2 \beta_{to}^4 \beta_{zo} q_B^2 e^{2x^2}}}{2\sqrt{2\mu_o e^2 J_{m-s}^2 (k_n R_o) \mu_1 (\sqrt{3\mu_1 + \mu_d}) Q_1}}$$
(17)

where $\mu_1 = \pi \beta^2_{to} L_1/\beta_{zo} \lambda$ is the normalized interaction length of the bunching cavity, μ_d is the normalized drift length, Q_1 is the bunching cavity Q factor, and $x = (\omega_o - \Omega) L_1/4v_{zo}$ the bunching cavity magnetic field detuning parameter. The other parameters are defined above. Typical choices for μ_1 and μ_d are 2 and 3, respectively. Assuming the same mode, magnetic field and beam parameters in the bunching and power cavities, and $Q_1 = 200$, one obtains $P_{in} = 530$ kW as the power required to phase-lock a gyrotron oscillator with an output power of over 160 MW for an effective gain of over 24 dB.

IV. CONCLUSIONS

A time slow-time-scale theory and a computer code for numerical calculations have been developed to investigate pulsed free-running and phase-locked gyrotrons. This code is expected to be a valuable resource for the design and interpretation of planned phase-locked gyrotron experiments. The calculations presented here show the feasibility of observing phase-locked operation with 50 nsec pulses. Phase-locking over a significant bandwidth is shown to be possible with a locking power 24 dB less than the oscillator output power for a single prebunching cavity. The effect of voltage ripple has been investigated and shown not to prevent phase-locked operation, however, applications requirements for rf phase control may place significant limits on allowable voltage ripple.

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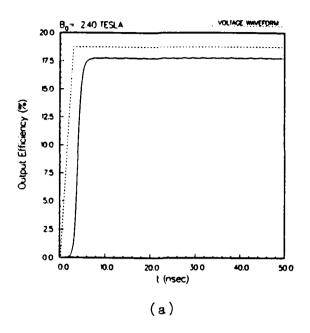
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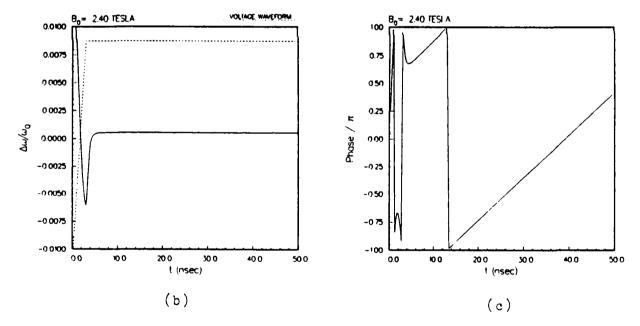
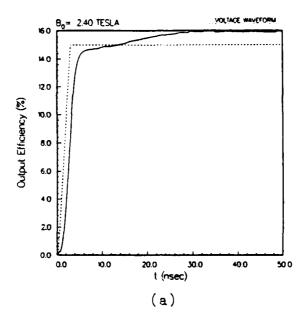


Figure 1



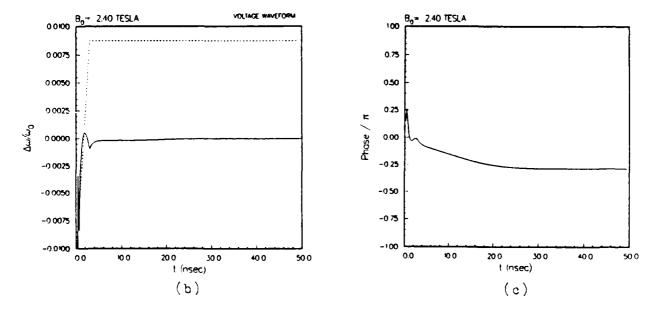
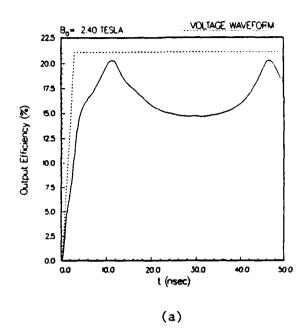


Figure 2



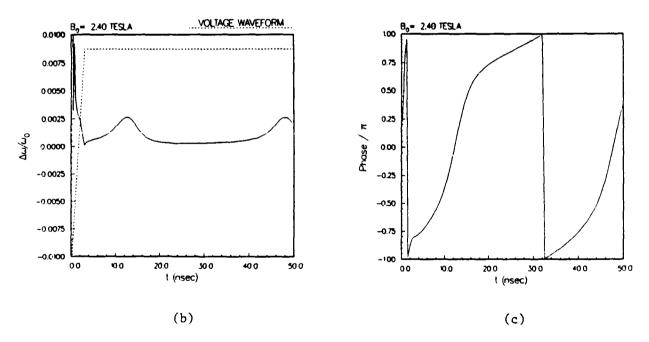
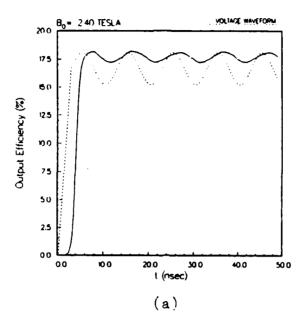


Figure 3



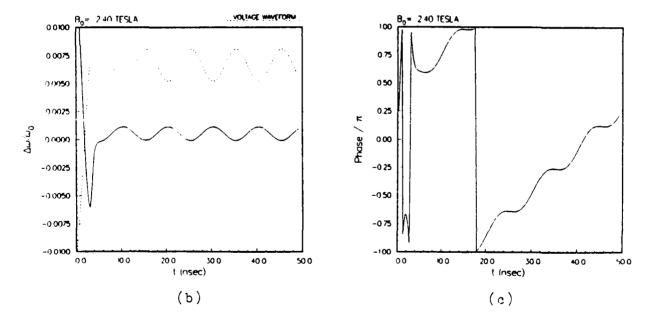
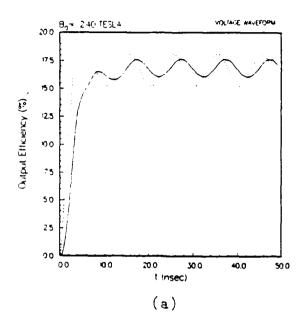


Figure 4



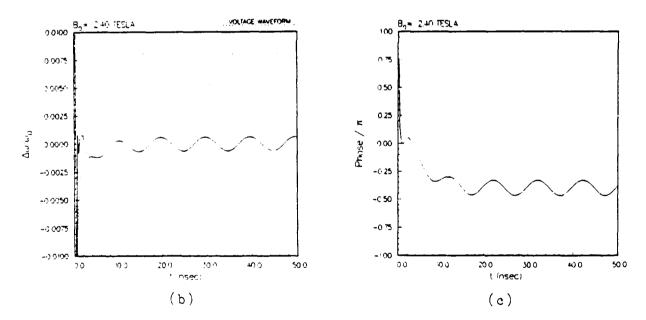
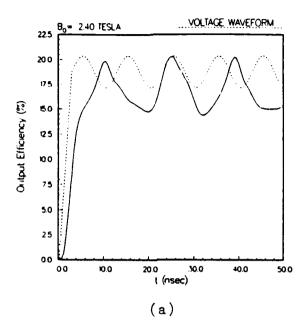


Figure 5



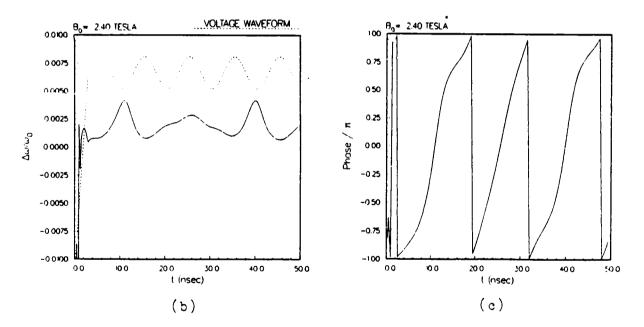


Figure 6

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